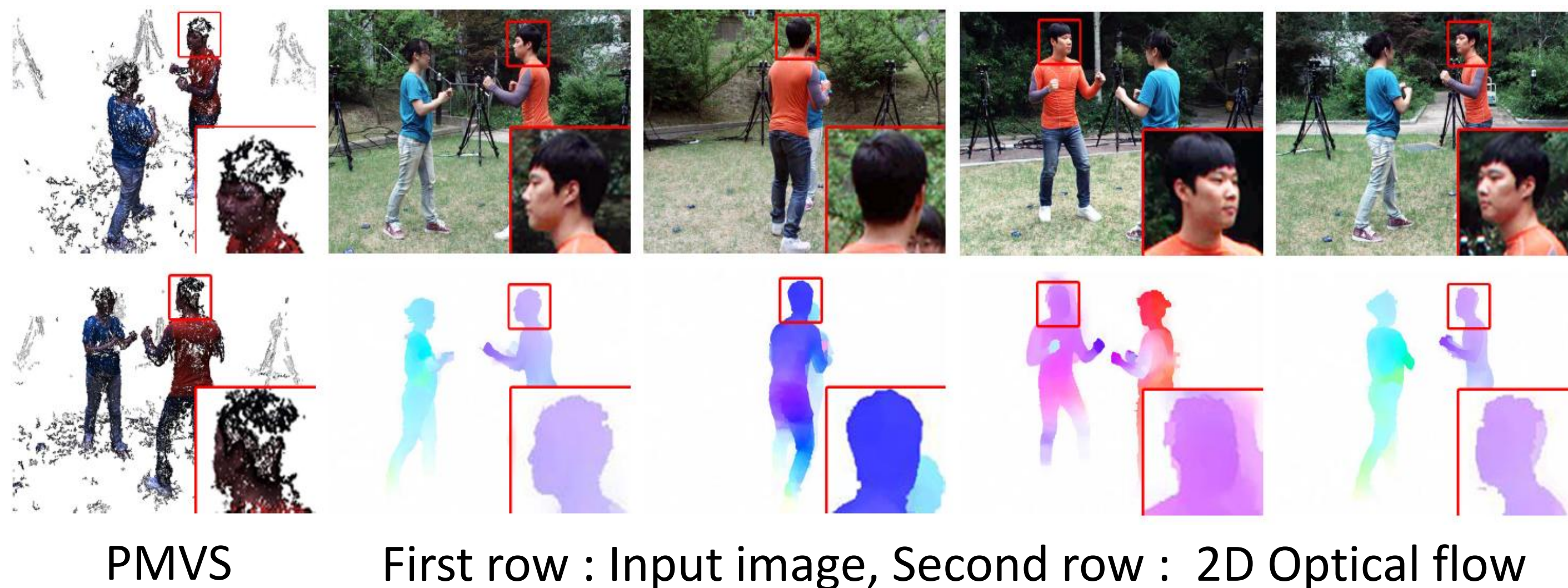


Introduction

- **Scene flow** is a dense 3D motion vector field which describes motion of objects in 3D world.
- There are many previous works use stereoscopic inputs whereas the estimated scene flow is 2.5D; In this work, we use multi-view data to estimate a complete 3D scene flow.
- We extend the **closed form tensor voting** (Wu *et al.* CVPR2010) to scene flow estimation and refinement
- Our approach processes directly on 3D point cloud which is model free and memory efficient

Scene Flow Estimation

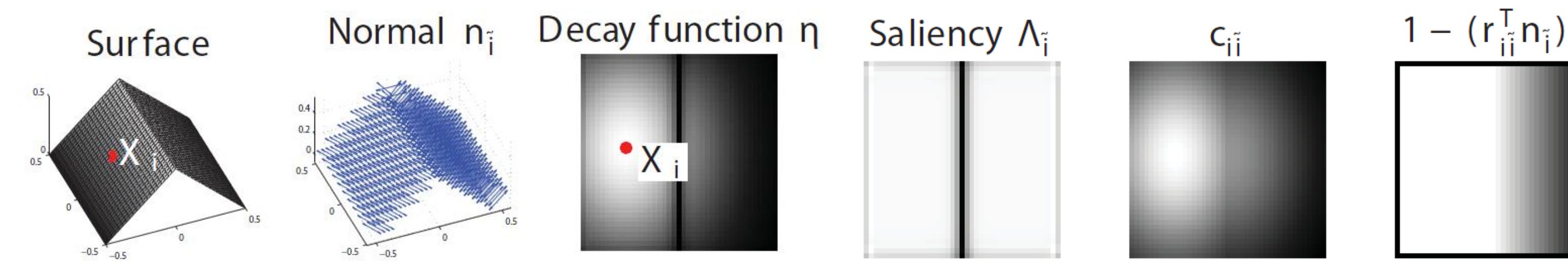


We estimate 3D geometry \mathbf{X}_i and 3D scene flow \mathbf{F}_i by using

- Patch based multi-view stereo (PMVS) (Furukawa *et al.* PAMI 2010)
- 2D Optical flow (Sun *et al.* CVPR 2010)
- Triangulation using direct linear transform (Vedula *et al.* PAMI 2005)

This method gives reasonable initialization, but not accurate enough.

Refinement of estimated Scene Flow



We regard $\mathbf{F}_i = m_i \vec{\mathbf{F}}_i$ and refine it by two steps:

Step 1: Refine direction vector, $\vec{\mathbf{F}}_i$ using closed form tensor voting [19,25]

$$\mathbf{S}_{i\bar{i}} = \eta(\mathbf{X}_i, \mathbf{X}_{\bar{i}}, \mathbf{n}_i, \mathbf{n}_{\bar{i}}) \vec{\mathbf{F}}_i \vec{\mathbf{F}}_{\bar{i}}^T$$

$$\eta(\mathbf{X}_i, \mathbf{X}_{\bar{i}}, \mathbf{n}_i, \mathbf{n}_{\bar{i}}) = c_{i\bar{i}} [\Lambda_i (1 - (\mathbf{r}_{i\bar{i}}^T \mathbf{n}_i)^2) + \Lambda_{\bar{i}} (1 - (\mathbf{r}_{i\bar{i}}^T \mathbf{n}_{\bar{i}})^2)]$$

where $c_{i\bar{i}}$ is Euclidean distance and $\Lambda_i = \lambda_{1,i} - \lambda_{2,i}$ is surface saliency of \mathbf{X}_i . $\Lambda_{\bar{i}}$ is also defined in similar manner.

Step 2: Refine magnitude m_i by minimizing

$$E(m_i) = \frac{1}{\mathbf{X}_{\sigma,i}^2} \|\mathbf{X}_{\mu,i} - (\mathbf{X}_i + m_i \vec{\mathbf{F}}_i)\|^2 + \kappa \sum_{\bar{i}} \eta(\mathbf{X}_i, \mathbf{X}_{\bar{i}}, \mathbf{n}_i, \mathbf{n}_{\bar{i}}) \|m_i - m_{\bar{i}}\|^2$$

where $\mathbf{X}_{\mu,i}$ and $\mathbf{X}_{\sigma,i}^2$ are mean and variance of 3D points which are adjacent to the ray $(\mathbf{X}_i + m_i \vec{\mathbf{F}}_i)$.

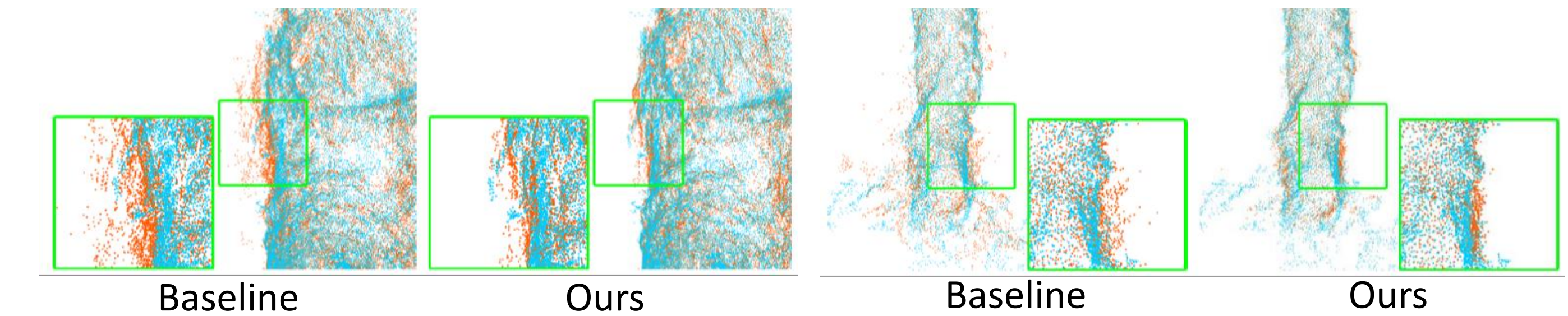
Note: to improve temporal coherency of the estimated scene flow, the voting field includes tensors in t-1, t+1 frames.

References

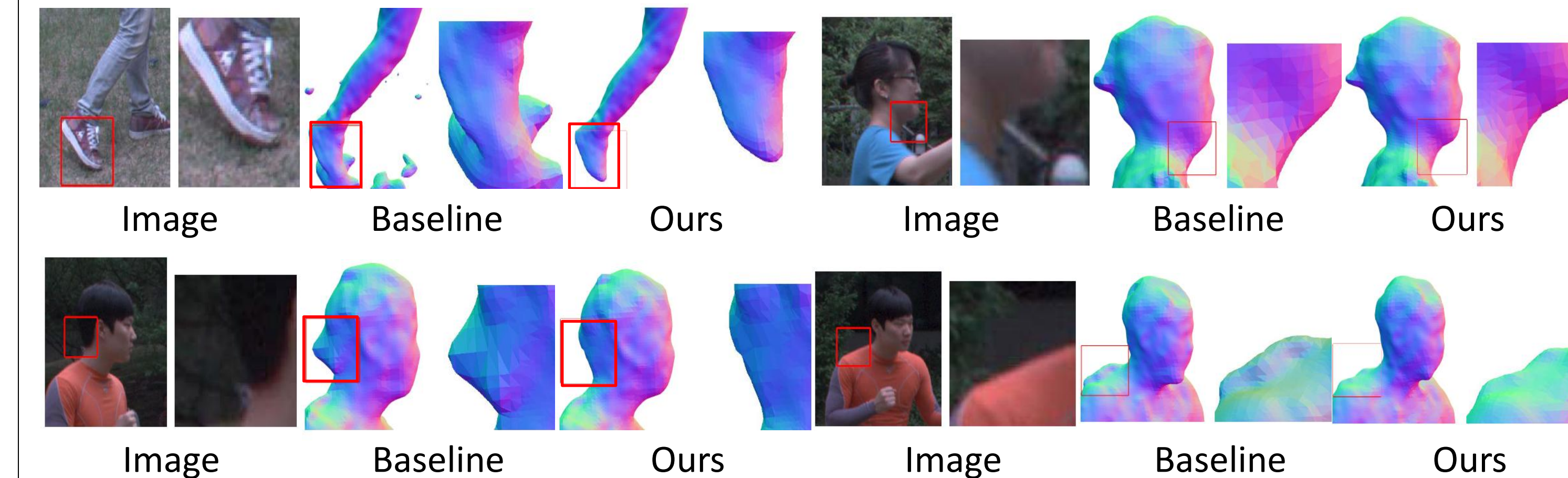
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Experiment on Real-world Dataset

Validation #1 : Point Clouds Overlapping using Refined flow



Validation #2 : 3D Reconstruction using Refined Flow



Experiment on Synthetic Dataset

Method	Measurement	$NRMS_X$ (%)	$NRMS_F$ (%)	AAE_F (deg)
Huguet <i>et al.</i> (ICCV2007)	w/o Discontinuities	9.82	15.96	7.17
	w/o Occlusions	1.19	11.04	6.66
	All pixels	10.43	19.09	9.20
Basha <i>et al.</i> (CVPR2010)	w/o Discontinuities	0.65	2.94	1.32
	w/o Occlusions	1.99	5.63	2.09
	All pixels	4.39	9.71	3.39
Ours (Baseline)	w/o Discontinuities	0.25	6.43	4.74
	w/o Occlusions	0.26	6.99	4.98
	All pixels	1.12	7.89	5.28
Ours (After Refinement)	w/o Discontinuities	0.23	4.88	2.73
	w/o Occlusions	0.24	5.07	2.72
	All pixels	0.57	5.42	2.83

* $NRMS$: normalized root mean square, AAE : Absolute angular error

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